

# Experiment Study of $f_0(975)$ in $J/\psi$ Decays

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Based on  $7.8 \times 10^6$   $J/\psi$  events collected by the BES at BEPC, the hadronic decays  $J/\psi \rightarrow \phi\pi^+\pi^-$  and  $J/\psi \rightarrow \omega\pi^+\pi^-$  are studied, and the branching ratios of these process and the mass and width of  $f_0$  are obtained. The angular distribution of  $J/\psi \rightarrow \phi f_0$ ,  $f_0 \rightarrow \pi^+\pi^-$  is fitted and the helicity amplitude ratios of this process are given for the first time.

**Key words:** scalar meson, threshold effect, spin-parity, helicity.

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## 1. INTRODUCTION

The behaviors and properties of  $0^{++}$  scalar mesons are the topic people have been interested in.  $f_0(975)$  is one of these scalar mesons.

The  $f_0$  was observed for the first time by  $\pi^-p \rightarrow n\pi^+\pi^-$  reaction in 1973 [1], and the clear  $f_0$  signal was also found in later  $e^+e^-$  collider experiments. Mark II [2] studied the inclusive  $J/\psi$  decay ( $J/\psi \rightarrow \pi^+\pi^- + X$ ) in 1981 and gave the  $f_0$  parameters as:

$$m = (974 \pm 4) - i(14 \pm 5)\text{MeV}.$$

In 1988 and 1989, DM2 [3] and Mark III [4] reported the results of exclusive channels  $J/\psi \rightarrow \phi f_0$ ,  $f_0 \rightarrow \pi^+\pi^-$ , respectively. The obvious  $f_0$  signal was observed and the branching ratio was given:

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$$(Br(J/\psi \rightarrow \phi f_0) \times Br(f_0 \rightarrow \pi^+\pi^-))_{DM2} = (2.4 \pm 0.2 \pm 0.4) \times 10^{-4};$$

$$(Br(J/\psi \rightarrow \phi f_0) \times Br(f_0 \rightarrow \pi^+\pi^-))_{MARKIII} = (4.2 \pm 0.3 \pm 0.6) \times 10^{-4}.$$

For decay channel  $J/\psi \rightarrow \omega\pi^+\pi^-$ , a small signal near 1 GeV was seen in the invariant mass spectrum of the  $\pi^+\pi^-$  system recoiling against the  $\omega$  by DM2 collaboration. They fit this spectrum in 900-1400 MeV range using an incoherent sum of two Breit-Wigner functions over a polynomial background, setting the  $f_0$  width to 35 MeV, and obtained

$$m = 959.4 \pm 6.5 \text{ MeV},$$

$$Br(J/\psi \rightarrow \omega f_0) \times Br(f_0 \rightarrow \pi^+\pi^-) = (1.10 \pm 0.21 \pm 0.16) \times 10^{-4}.$$

Mark III found only a small enhancement near  $f_0$  mass in channel  $J/\psi \rightarrow \omega\pi^+\pi^-$  and didn't give out the mass and width.

According to these experimental results, many theorists have made efforts to understand the scalar "meson"  $f_0$ . However, after about 20 years' controversy, the nature of  $f_0$  is still not settled. Is  $f_0$  just the  $s\bar{s}$  meson [5], the multiquark state [6], or the  $K\bar{K}$  molecular bound state? [7] Therefore, further experimental studies for the  $f_0$  are of great meaning in understanding the nature of  $f_0$ .

Based on  $7.8 \times 10^6$   $J/\psi$  events collected by BES detector at BEPC, we studied the channels  $J/\psi \rightarrow \phi\pi^+\pi^-$  and  $J/\psi \rightarrow \omega\pi^+\pi^-$  systematically. The branching ratios of these two processes and the mass and width of  $f_0$  were given. After fitting the angular distribution of  $J/\psi \rightarrow \phi f_0$ ,  $f_0 \rightarrow \pi^+\pi^-$ , the helicity amplitude ratio of this process was obtained for the first time. These experimental results will no doubt provide information in understanding  $f_0$ .

## 2. $J/\psi \rightarrow \phi f_0$ , $f_0 \rightarrow \pi^+\pi^-$

### 2.1. Event Selection

In the four-prong events, obtained after general offline processing, the net charge of four charged tracks  $\sum_{i=1}^4 Q_i$  is required to be zero. The vector sum of four charged tracks is required to be less than 0.3 GeV. The vertex cuts are:  $|x| < 6$  mm,  $|y| < 6$  mm, and  $|z| < 80$  mm.

At least one charged track is determined to be a kaon within  $3\sigma$  by time of Flight Counter (TOF) or DEDX ( $dE/dx$  of main drift chamber) measurement. Four-constraint kinematic fits are performed for all possible  $K^+K^-\pi^+\pi^-$  combinations, and the combination with least  $\chi^2$  is assumed to be the correct one. If only one charged track is determined to be a kaon within  $3\sigma$  by TOF or DEDX measurement,  $\chi^2 < 7$  is required, and if at least two charged tracks are determined to be kaons within  $3\sigma$  by TOF or DEDX measurement,  $\chi^2 < 25$  is required. We analyzed about  $7.8 \times 10^6$   $J/\psi$  events from run 462-961, run 1248-1616, run 1750-1940, and run 3579-3739, according to the preceding event selection criteria.

### 2.2. The Fitting of $\pi^+\pi^-$ Invariant Mass Spectrum Recoiling Against $\phi$

Figure 1 shows the invariant mass spectrum of  $\pi^+\pi^-$  system in  $J/\psi \rightarrow \phi\pi^+\pi^-$ . An obvious  $f_0$  signal near 1 GeV with a steep fall on the high mass side can be observed. To consider the asymmetry of spectrum due to  $K\bar{K}$  threshold effect, the coupled-channel fitting formula [8] is adopted to fit the signal  $f_0$  by using the Maximum Likelihood method:

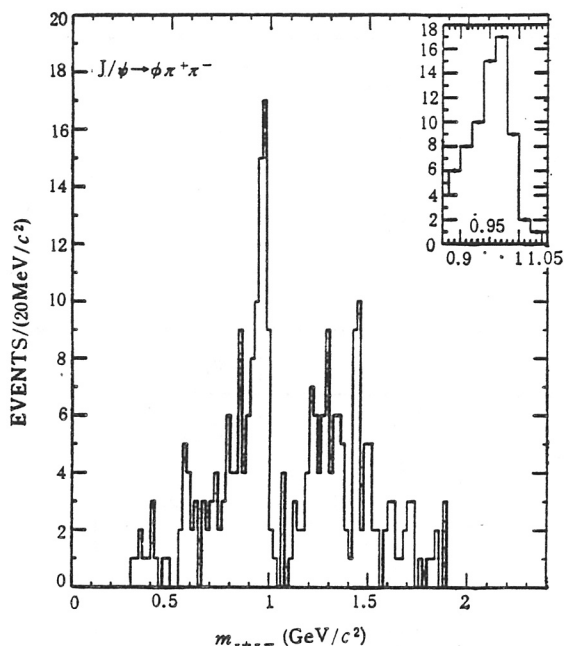


Fig. 1

$\pi^+\pi^-$  invariant mass spectrum recoiling against  $\phi$ .

$$\frac{d\sigma}{dm} \sim \frac{\Gamma_\pi}{|m_R^2 - m^2 - im_R(\Gamma_\pi + \Gamma_K)|^2},$$

where  $m_R$  is the resonance mass,

$$\Gamma_\pi = g_\pi \sqrt{\frac{m^2}{4} - m_\pi^2}, \quad \Gamma_K = \begin{cases} g_K \sqrt{\frac{m^2}{4} - m_K^2} & \text{above threshold} \\ ig_K \sqrt{\frac{m^2}{4} - m_K^2} & \text{below threshold} \end{cases},$$

$g_\pi$  and  $g_K$  are the coupling constants for  $f_0 \rightarrow \pi^+\pi^-$  and  $f_0 \rightarrow K^+K^-$ , respectively.

From the results of Monte Carlo simulation, the acceptance in  $f_0$  mass range is almost uniform, and the mass resolution  $\sigma_m = 10$  MeV.

The fitted results for the mass and width of  $f_0$  are:  $m = 969 \pm 4$  MeV,  $\Gamma = 43 \pm 8$  MeV.

### 2.3. Branching Ratio of $J/\psi \rightarrow \phi f_0$

From the fitting of  $\pi^+\pi^-$  invariant mass spectrum, 59  $f_0$  events are obtained. The efficiency given by Monte Carlo simulation is about 10%, and the total  $J/\psi$  events are  $7.8 \times 10^6$ . Therefore, the branching ratio of this process is:  $Br(J/\psi \rightarrow \phi f_0) = (2.9 \pm 0.4 \pm 0.5) \times 10^{-4}$ .

### 2.4. Angular Distribution of $J/\psi \rightarrow \phi f_0$

For the strong decay process  $J/\psi \rightarrow V + X$ ,  $V \rightarrow P_1^+ P_2^-$ ,  $X \rightarrow P_3^+ P_4^-$ , the helicity of the angular distribution is [9]:

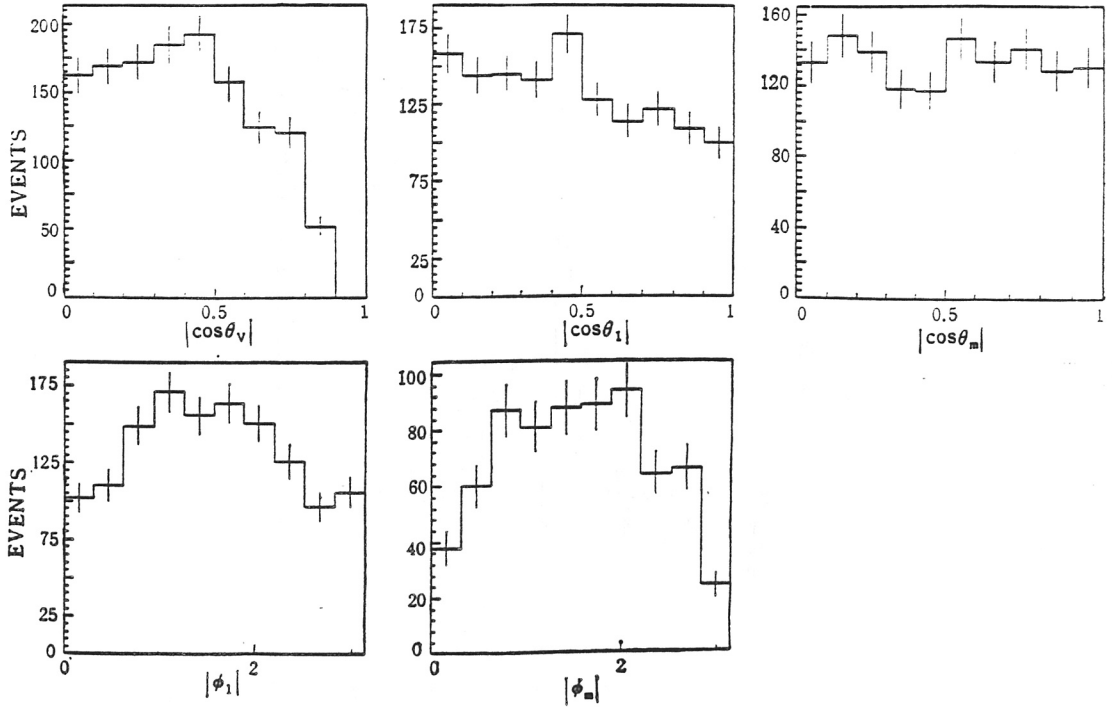


Fig. 2

The detection efficiency for the decay  $J/\psi \rightarrow \phi f_0$ ,  $f_0 \rightarrow \pi^+ \pi^-$  versus different angles. The meanings of  $\theta_v$ ,  $\theta_1$ ,  $\theta_m$ ,  $\phi_1$ , and  $\phi_m$  refer to the text.

$$W(\theta_v, \theta_1, \phi_1, \theta_m, \phi_m) \sim \sum I_{\lambda_j, \lambda_j'}(\theta_v) \cdot A_{\lambda_v \lambda_X} \cdot A_{\lambda_v' \lambda_X'} \cdot D_{\lambda_v, 0}^{1*}(\theta_1, \phi_1, 0) \cdot D_{\lambda_v', 0}^{1*}(\theta_1, \phi_1, 0) \cdot D_{\lambda_X, 0}^{1*}(\theta_m, \phi_m, 0) \cdot D_{\lambda_X', 0}^{1*}(\theta_m, \phi_m, 0),$$

in which  $S$  is the spin of  $X$ ,  $A_{\lambda_v \lambda_X}$  is the helicity amplitude of  $e^+e^- \rightarrow J/\psi \rightarrow V + X$ ,  $\theta_v$  is the angle between directions of meson  $V$  and  $e^+$  beam in  $J/\psi$  static frame, and  $(\theta_1, \phi_1)$  and  $(\theta_m, \phi_m)$  are the polar and azimuthal angles of  $P_1^+$  and  $P_3^+$  in meson  $V$  and  $X$  centers of mass systems, respectively. The ratios of helicity amplitudes are defined as:

$$x = \frac{A_{11}}{A_{10}}, \quad y = \frac{A_{12}}{A_{10}}, \quad z_1 = \frac{A_{00}}{A_{10}}, \quad z_2 = \frac{A_{01}}{A_{10}},$$

If  $X$  is a scalar meson, we have

$$W \sim (1 + \cos^2 \theta_v) \sin^2 \theta_1 - \sin^2 \theta_v \sin^2 \theta_1 \cos(2\phi_1) + 2 \sin^2 \theta_v \cos^2 \theta_1 z_1^2 - 2 \sin 2\theta_v \sin \theta_1 \cos \theta_1 \cos \phi_1 z_1,$$

By using the method of helicity analysis [10], we fit the angular distribution of decay  $J/\psi \rightarrow \phi f_0$ ,



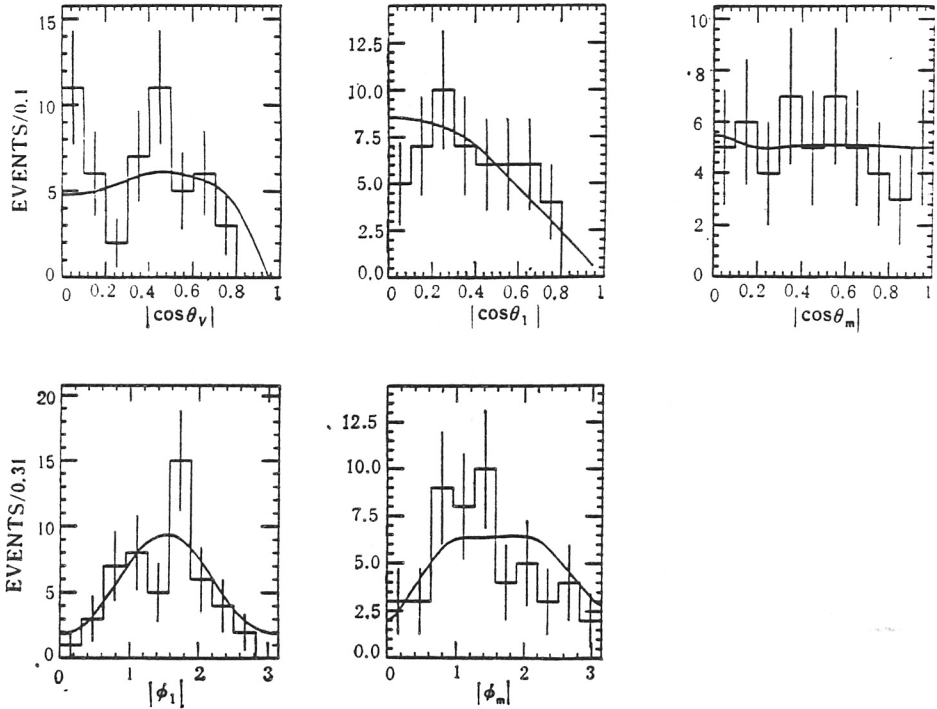


Fig. 3

The angular distribution of the decay  $J/\psi \rightarrow \phi f_0$ ,  $f_0 \rightarrow \pi^+ \pi^-$ . The data are represented by histograms and the fit results by curves.

$f_0 \rightarrow \pi^+ \pi^-$ . The angular resolution function can be treated as a  $\delta$  function because of the good position resolution of the main drift chamber of BES. The efficiency curves from Monte Carlo simulations are shown in Fig. 2 and the angular distributions of data and the results of fitting are shown in Fig. 3. From the uniform distribution of  $\cos \theta_m$ , we get the conclusion of  $f_0$  being a  $0^{++}$  scalar meson. The maximum likelihood fitting results in the parameter value of  $z_1 = 0.09 \pm 0.18$ .

### 3. $J/\psi \rightarrow \omega f_0$ , $f_0 \rightarrow \pi^+ \pi^-$

#### 3.1. Event Selection

In the four-prong events, the net charge of four charged tracks  $\sum_{i=1}^4 Q_i$  is required to be zero. We also require the number of neutral tracks to be two to six. TOF and DEDX measurements are used to identify particles. The maximum weight of charged  $\pi$ 's must satisfy  $W_{\pi}^{\max} > 0.95$ . In the kinematic fitting, we assume any two of the neutral tracks and four charged tracks to be  $\gamma\gamma$  and  $2(\pi^+ \pi^-)$ , respectively, and then perform 4C-fit  $\chi^2 < 50$ , select the combination with the least  $\chi^2$  as the needed combination  $2(\pi^+ \pi^-)\gamma\gamma$ . The  $\pi^0$  is selected by the cut  $|m_{\gamma\gamma} - 0.135| < 0.06$  GeV and then the  $\omega$  is selected by the cut:

$$|m_{\pi^+ \pi^- \pi^0} - 0.783| < 0.06 \text{ GeV}.$$

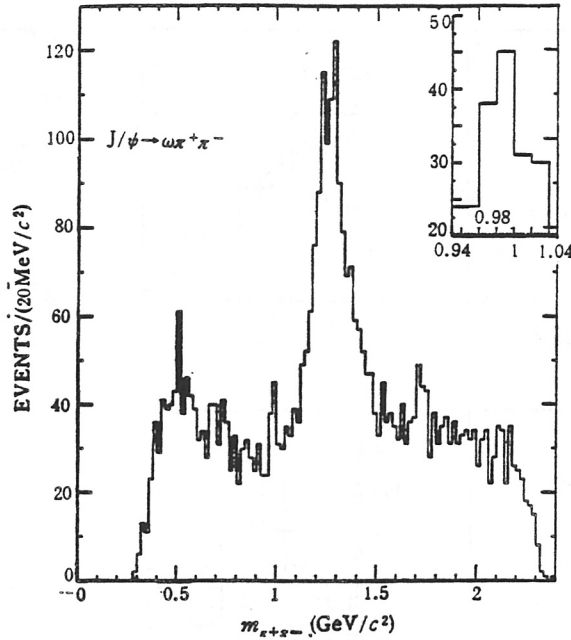


Fig. 4

$\pi^+\pi^-$  invariant mass spectrum recoiling against  $\omega$ .

Based on the preceding event selection criteria, we analyzed  $7.8 \times 10^6$   $J/\psi$  events from run 462-961, run 1248-1616, run 1750-1940, and run 3579-3739.

### 3.2. $\pi^+\pi^-$ Invariant Mass Spectrum Recoiling Against $\omega$

From the  $\pi^+\pi^-$  invariant mass spectrum recoiling against  $\omega$ , shown in Fig. 4, we can see that there is a clear accumulation of events at the mass near 1 GeV. By taking into account the mass resolution near 1 GeV  $\sigma_m = 10$  MeV, obtained from Monte Carlo simulation, and fitting the whole mass range using five incoherent B-W functions over a polynomial background, the parameters of  $f_0$  are given as:  $m_{f_0} = 985 \pm 9$  MeV,  $\Gamma_{f_0} = 11 \pm 6$  MeV.

Because the efficiency in  $f_0$  range by Monte Carlo is about 7.1% and the total  $f_0$  events is 32, the branching ratio can be calculated as:  $Br(J/\psi \rightarrow \omega f_0) = (1.3 \pm 0.8 \pm 0.2) \times 10^{-4}$ .

## 4. CONCLUSIONS

We have investigated the  $\pi^+\pi^-$  invariant mass spectrum from  $J/\psi \rightarrow \phi \pi^+\pi^-$  and  $J/\psi \rightarrow \omega \pi^+\pi^-$ . The  $f_0$  signals were observed in both channels. The fitting results show that the position of  $f_0$  recoiling against  $\phi$  is lower than its position of recoiling against  $\omega$ , whereas the width is larger. Are these two  $f_0$ s the same state? From the theoretical point of view, if these two  $f_0$ s are considered as the same state, the assumption of  $f_0$  as a  $s\bar{s}$  state cannot explain the appearance of  $f_0$  in  $J/\psi \rightarrow \omega \pi^+\pi^-$ , although it explains the  $f_0$  in  $J/\psi \rightarrow \phi f_0$  well. On the other hand, we can consider the same problem for  $f_0$ 's partner  $a_0$ . In  $J/\psi \rightarrow \gamma K^+ K^- \pi^0$  channel, there is an obvious  $\iota(1440)$  peak in  $K\bar{K}\pi^0$  mass spectrum and a clear  $a_0(980)$  in  $K\bar{K}$  mass spectrum. It can be deduced that this  $a_0(980)$  comes from the decay of  $\iota(1440)$ . However, in channel  $J/\psi \rightarrow \gamma \eta \pi^+\pi^-$ , there exists a clear  $a_0$  in the  $\eta \pi$  spectrum, but no  $\iota(1440)$  in the

$\eta\pi\pi$  mass spectrum. Therefore, this  $a_0$  does not come from  $\iota(1440)$  decay, and we have the same question, that is, are these  $a_0$ s the same state? Our results are still preliminary. More channels and more statistics are needed to study  $f_0$  carefully.

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## APPENDIX

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