

Discovery prospects for a leptophilic gauge boson Z_ℓ at CEPC and ILC

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Abstract: We investigate the discovery prospects of a leptophilic gauge boson Z_ℓ at future e^+e^- colliders, focusing on a comparative study of the Circular Electron–Positron Collider (CEPC) and the International Linear Collider (ILC). Such a state naturally arises from an additional $U(1)_\ell$ gauge symmetry, under which quarks remain neutral while all leptons carry a universal charge, motivated by neutrino oscillations and scenarios of physics beyond the Standard Model. As a clean benchmark, we study the process $e^+e^- \rightarrow \mu^+\mu^-$, including realistic effects of initial-state radiation and beamstrahlung. Our results indicate that the CEPC, with its very high luminosity at $\sqrt{s} = 240$ GeV, can probe couplings down to $g_\ell \approx 10^{-3}$ for Z_ℓ masses up to about 220 GeV. The ILC extends the sensitivity to heavier states in the multi-hundred GeV range through its higher \sqrt{s} stages. These findings demonstrate the strong complementarity of circular and linear colliders in exploring purely leptophilic interactions.

Keywords: leptophilic gauge boson, Z_ℓ , CEPC, ILC, electron–positron collider, beyond standard model

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I. INTRODUCTION

The Standard Model (SM) of particle physics has been remarkably successful in describing the fundamental constituents of matter and their interactions [1]. Nevertheless, the observation of neutrino oscillations [2, 3] and the violation of individual lepton flavor numbers clearly point toward new physics beyond the SM. Among the simplest and most intriguing possibilities is the existence of an additional abelian gauge symmetry, under which quarks remain neutral while all leptons carry a universal charge. Such a symmetry is particularly motivated by the fact that neutrino oscillations already require new dynamics in the lepton sector, suggesting that leptons may play a privileged role in extensions of the SM. In addition, the $U(1)_\ell$ construction is anomaly-free when all lepton families are assigned identical charges, providing a theoretically consistent and minimal extension of the gauge structure. The associated gauge boson, conventionally denoted as the leptophilic photon Z_ℓ , couples exclusively to leptons and realizes a genuinely leptophilic interaction [4–10].

Electron–positron colliders provide an ideal environment to probe this type of new physics due to their clean experimental conditions and well-defined initial states. In particular, the upcoming Circular Electron–Positron Collider (CEPC) [11] and the International Linear Collider

(ILC) [12] represent two complementary approaches for the next generation of lepton colliders. While the CEPC aims at extremely high luminosity around the Higgs factory energy, the ILC offers the flexibility of operating at both $\sqrt{s} = 250$ GeV and 500 GeV to extend the reach into the TeV regime. This complementarity renders them powerful and mutually reinforcing facilities to explore new leptophilic interactions.

Beyond the general motivation, it is worth noting that the CEPC and ILC offer complementary advantages that have not yet been systematically compared in a leptophilic context. Earlier works have focused either on generic Z' scenarios, including quark couplings or on simplified parton-level estimates for purely leptophilic interactions [7, 8], without incorporating realistic collider and detector effects. In contrast, the present study includes both initial-state radiation (ISR) and beamstrahlung (BS) as well as acceptance cuts to provide sensitivity projections that are directly applicable to the experimental programs of the CEPC and ILC.

The comparison is timely in view of the global strategy for future colliders. The CEPC has been highlighted as a central project in China, designed to operate as a Higgs factory with unprecedented luminosity. The ILC has received strong international attention as a linear machine with higher center-of-mass energy options. Establishing the relative strengths of these colliders in prob-

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ing leptophilic gauge interactions is not only of theoretical interest but also of practical importance for optimizing the physics reach of upcoming facilities. This complementarity is particularly relevant since hadron colliders have very limited sensitivity to leptophilic states, making lepton machines unique laboratories for such searches.

Taken together, these considerations underscore both the novelty and significance of the present analysis. Our results provide the first direct, side-by-side comparison of CEPC and ILC capabilities for discovering a leptophilic photon, contributing to the broader discussion of physics opportunities at next-generation lepton colliders.

In this study, we present a comparative phenomenological study of the discovery potential for the leptophilic photon Z_ℓ at the CEPC and ILC, focusing on the clean channel $e^+e^- \rightarrow \mu^+\mu^-$. We evaluate the expected sensitivities by incorporating realistic effects of ISR, BS, and detector acceptance. This channel provides a distinctive signature with minimal SM background and constitutes an optimal probe of purely leptophilic interactions. In this way, our analysis extends previous parton-level estimates [7, 8] and offers a more reliable assessment of the capabilities of future e^+e^- colliders.

II. THEORETICAL FRAMEWORK

A minimal and economical way to extend the SM is to introduce an additional abelian gauge symmetry $U(1)'_\ell$ under which all leptons carry a universal charge, while quarks remain neutral. This idea dates back to early studies of generalized gauge structures [13–15] and has been revisited in various contexts of leptophilic or leptonic interactions [8, 9, 16]. The new gauge boson, denoted as Z_ℓ , couples exclusively to leptons and therefore realizes a genuinely leptophilic interaction.

The covariant derivative is modified to include the new gauge interaction

$$D_\mu = \partial_\mu + ig'_\ell q_\ell Z'_\mu, \quad (1)$$

where g'_ℓ is the gauge coupling constant, q_ℓ the universal lepton charge, and Z'_μ the new gauge field. The relevant terms of the Lagrangian read

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \bar{\ell}i\gamma^\mu D_\mu \ell + (D_\mu \Phi)^\dagger (D^\mu \Phi) - V(\Phi), \quad (2)$$

where Φ is a scalar field charged under $U(1)'_\ell$ whose vacuum expectation value (vev) spontaneously breaks the new symmetry to generate a mass for the leptophilic boson Z_ℓ .

The interaction between Z_ℓ and the leptonic current can be expressed as

$$\mathcal{L}_{\text{int}} = g_\ell Z_{\ell,\mu} J_{\text{lep}}^\mu, \quad J_{\text{lep}}^\mu = \sum_{\ell=e,\mu,\tau} \bar{\ell} \gamma^\mu \ell, \quad (3)$$

which highlights the universal coupling of Z_ℓ to all charged leptons. A crucial theoretical requirement is the absence of gauge anomalies, which would otherwise spoil the consistency of the theory at the quantum level [17–20]. In the present setup, anomalies are cancelled if all three lepton families are assigned the same $U(1)'_\ell$ charge. With this choice, the $[SU(2)_W]^2 U(1)'_\ell$, $[U(1)_Y]^2 U(1)'_\ell$, and $[U(1)'_\ell]^3$ anomalies vanish.

Mixing effects can, in principle, arise in two ways. First, kinetic mixing with the hypercharge gauge boson B_μ may occur through

$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2} F_{\mu\nu}^Y F'^{\mu\nu}, \quad (4)$$

where ϵ parametrizes the mixing strength. Such terms are typically induced at the loop level [14], but precision electroweak data require $\epsilon \lesssim 10^{-2}$ [7]. Recent works [21] have studied electroweak precision constraints in nearly-degenerate Z' – Z systems, showing that even small kinetic and mass mixing generate observable shifts in the oblique parameters S, T, U , consistent with existing data. Second, after electroweak symmetry breaking, the SM Z boson and new Z_ℓ can mix via the scalar sector. The mass-squared matrix in the (Z, Z_ℓ) basis is

$$M^2 = \begin{pmatrix} M_Z^2 & \delta M^2 \\ \delta M^2 & M_{Z_\ell}^2 \end{pmatrix}, \quad (5)$$

with δM^2 induced by the vev of Φ . Further studies [22] computed corrections to electroweak observables from such mixings in the context of anomalies, such as the W -boson mass shift, finding constraints that closely match the $\theta \lesssim 10^{-3}$ limit. In the parameter space of interest, both kinetic and mass mixing are negligible; thus, Z_ℓ couples purely to leptons at the tree level. Model-independent analyses [23] further support the treatment of mixing effects as subdominant for the benchmark values considered.

Constraints from precision electroweak measurements imply a lower bound on the ratio between the new boson mass and its coupling,

$$\frac{M_{Z_\ell}}{g_\ell} \gtrsim 7 \text{ TeV}. \quad (6)$$

Representative exclusion limits on g_ℓ for benchmark masses are summarized in Table 1. Electroweak precision data require $g_\ell \lesssim 1.4 \times 10^{-2}$ at $M_{Z_\ell} \sim 100 \text{ GeV}$, with the bound gradually relaxing to $\mathcal{O}(10^{-1})$ in the multi-TeV

Table 1. 95% C.L. exclusion limits on the leptophilic coupling g_ℓ from electroweak precision fits.

M_{Z_ℓ}/GeV	Limit on g_ℓ
100	$< 1.4 \times 10^{-2}$
240	$< 3.4 \times 10^{-2}$
250	$< 3.6 \times 10^{-2}$
500	$< 7.1 \times 10^{-2}$
1000	$< 1.4 \times 10^{-1}$
3000	$< 4.3 \times 10^{-1}$

regime.

Together, the framework is anomaly-free, predictive, and renormalizable. The Z_ℓ couples universally to leptons, has negligible couplings to quarks, and only tiny mixing with SM gauge bosons. These features make future high-luminosity lepton colliders the ideal environment to search for Z_ℓ , as hadronic machines are comparatively much less sensitive.

III. COLLIDER SETUP

To assess the sensitivity to leptophilic interactions at future e^+e^- machines, we based our analysis on the baseline beam parameters summarized in Table 2. For the CEPC we adopted the design values reported in the Conceptual Design Report (2018) [11], while for the ILC we followed the Technical Design Report (2013) [12]; these choices are consistent with Ref. [24]. Throughout, σ_x and σ_y denote the horizontal and vertical root-mean-square (rms) beam sizes at the interaction point (IP), respectively, σ_z is the longitudinal bunch length (rms size in μm), N_b is the particles per bunch (in units of 10^{10}), and L is the integrated luminosity accumulated over the data-taking period. The CEPC is envisaged as a circular Higgs factory operating at $\sqrt{s} = 240$ GeV with a target integrated luminosity of approximately 6 ab^{-1} , providing a clean environment with very high statistics for precision Higgs and electroweak studies. In contrast, the ILC is a linear collider foreseen to begin at $\sqrt{s} = 250$ GeV (1.35 ab^{-1}) with an upgrade path to $\sqrt{s} = 500$ GeV (1.8 ab^{-1}) [12], thereby extending the direct kinematic reach for heavier states. Although other proposed lepton colliders such as FCC-ee [25] and CLIC [26] offer additional benchmark scenarios, they lie beyond the scope of the present CPC-focused comparison. Hence, in what follows, we restrict our quantitative analysis to the CEPC and ILC.

To obtain realistic sensitivity estimates, we included the effects of initial-state radiation (ISR) and beamstrahlung (BS), which modify the effective luminosity spectrum. The ISR is implemented following the structure-function approach of Skrzypek and Jadach [27, 28]. The BS is modeled using the official collider beam spec-

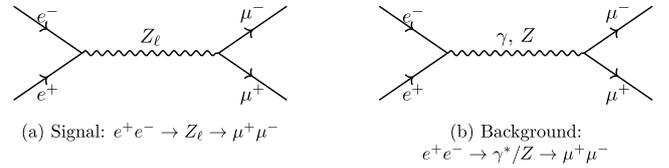
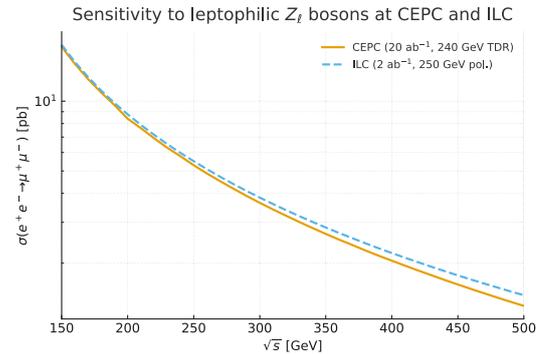
Table 2. Baseline beam parameters adopted for CEPC and ILC. Integrated luminosities are given in ab^{-1} .

Collider	\sqrt{s}/GeV	L/ab^{-1}	σ_x/nm	σ_y/nm	$\sigma_z/\mu\text{m}$	$N_b (\times 10^{10})$
CEPC	240	6.0	16.0	0.12	4.4	3.7
ILC-250	250	1.35	515.0	7.7	300.0	2.0
ILC-500	500	1.80	474.0	5.9	300.0	2.0

tra provided in the design reports [29]. These effects reduce the effective collision energy and broaden the invariant-mass distributions, affecting both total and differential cross sections. Throughout our study, we simulated the signal process $e^+e^- \rightarrow \mu^+\mu^-$ via $\gamma/Z/Z_\ell$ exchange and the corresponding SM background using the CalcHEP framework [30–32]. Detector effects are approximated by applying acceptance cuts of $|\cos\theta_\mu| < 0.95$ and assuming high muon identification efficiency consistent with design studies.

IV. SIGNAL AND BACKGROUND ANALYSIS

The signal process considered is $e^+e^- \rightarrow \mu^+\mu^-$, mediated by Z_ℓ . This channel is particularly advantageous because the muon final state can be reconstructed with high efficiency and excellent momentum resolution, making it the cleanest probe of leptophilic interactions.

**Fig. 1.** Representative Feynman diagrams for the signal process $e^+e^- \rightarrow Z_\ell \rightarrow \mu^+\mu^-$ (left) and the dominant SM background $e^+e^- \rightarrow \gamma^*/Z \rightarrow \mu^+\mu^-$ (right).**Fig. 2.** (color online) Total cross section $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ as a function of the center-of-mass energy \sqrt{s} for the CEPC and ILC benchmark configurations. The CEPC baseline at $\sqrt{s} = 240$ GeV with 20 ab^{-1} integrated luminosity provides excellent sensitivity to light leptophilic gauge bosons, while the higher-energy ILC stages (250 and 500 GeV) extend the accessible mass range to heavier Z_ℓ states.

The dominant irreducible background arises from the SM Drell–Yan production via photon and Z exchange, $e^+e^- \rightarrow \gamma^*/Z \rightarrow \mu^+\mu^-$. This background is theoretically well understood and experimentally clean, allowing deviations from the SM prediction to be directly attributed to the presence of a Z_ℓ contribution [33]. Reducible backgrounds from processes such as $e^+e^- \rightarrow \tau^+\tau^-$ or multihadronic final states are negligible once standard selection criteria are applied. For this reason, the di-muon channel provides a uniquely sensitive and robust avenue to search for a leptophilic photon at future lepton colliders. The

signal and background processes are illustrated in Fig. 1.

In our analysis, ISR and BS effects are included, as discussed in the previous section. Detector-level effects are approximated by applying acceptance cuts of $|\cos\theta_\mu| < 0.95$ and $p_T^\mu > 10$ GeV, consistent with the design reports of the CEPC and ILC. After cuts, the SM background is reduced while the Z_ℓ signal retains a significant fraction of events, enhancing sensitivity in the high-mass tails of distributions.

The statistical significance is evaluated using a binned likelihood method based on the invariant-mass spectrum.

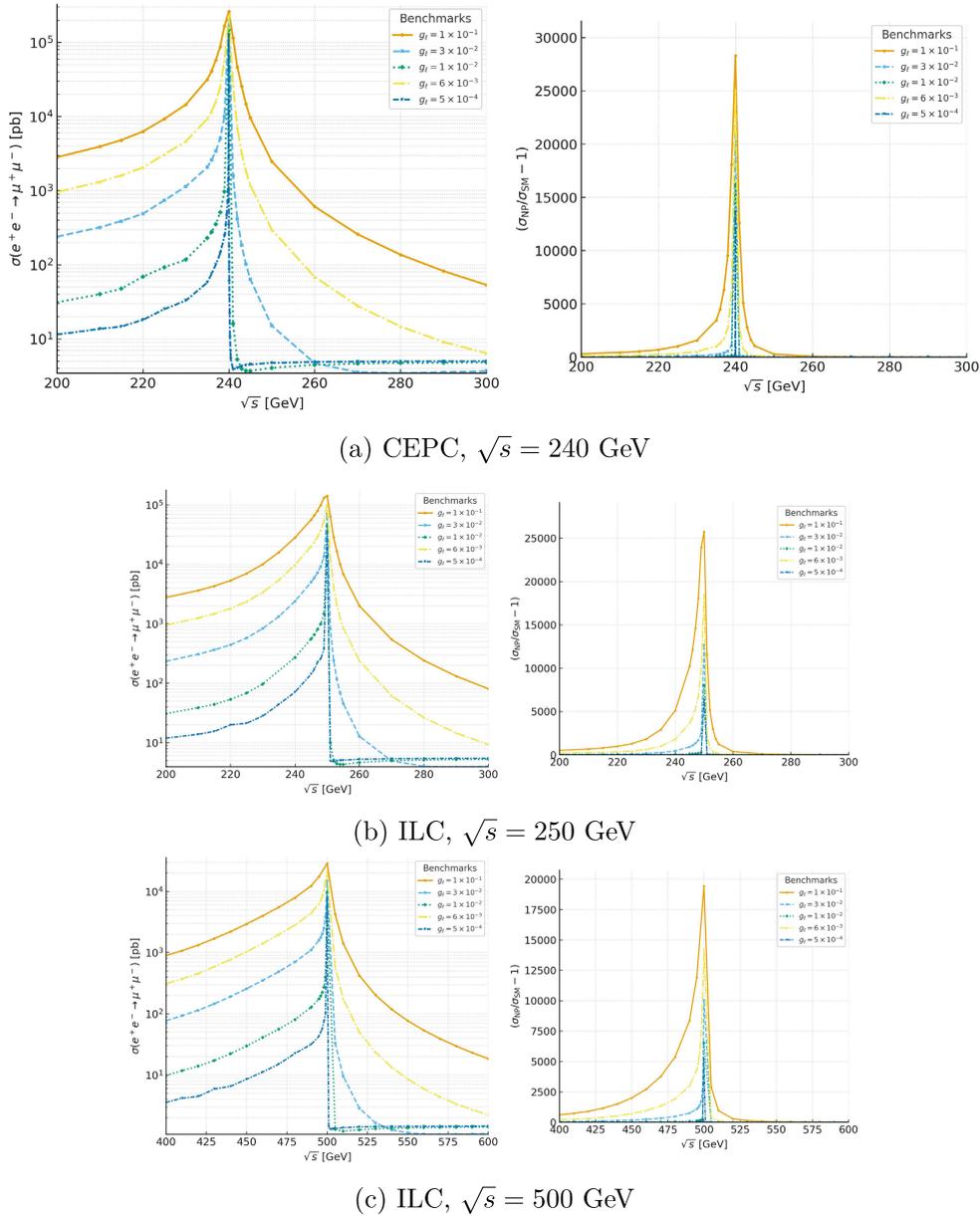


Fig. 3. (color online) Total cross section $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ and its relative deviation $(\sigma_{NP}/\sigma_{SM} - 1)$ as functions of M_{Z_ℓ} for representative couplings g_ℓ . (a) CEPC at $\sqrt{s} = 240$ GeV with 20 ab^{-1} integrated luminosity (TDR baseline). (b) ILC at $\sqrt{s} = 250$ GeV with 2 ab^{-1} polarized beams. (c) ILC at $\sqrt{s} = 500$ GeV, where higher energies extend the sensitivity to heavier Z_ℓ states. Right-hand panels show the fractional deviation from the SM prediction, highlighting the discovery potential even for small couplings.

For each benchmark mass hypothesis, we derived exclusion limits on the coupling g_ℓ at 95% C.L. [34, 35], the predicted signal-plus-background spectrum with the background-only expectation. These results are presented in the following section.

The energy dependence of the total cross section is displayed in Fig. 2. At the CEPC operating at $\sqrt{s} = 240$ GeV, the high luminosity allows excellent sensitivity to deviations from the SM prediction. The ILC at $\sqrt{s} = 250$ and 500 GeV extends the accessible range in energy and probes heavier Z_ℓ states. The comparison illustrates the complementarity of circular and linear machines in exploring leptophilic interactions.

In Fig. 3, we show the total cross section and the relative deviation $(\sigma_{\text{NP}}/\sigma_{\text{SM}} - 1)$ as functions of the new boson mass M_{Z_ℓ} for representative values of the coupling g_ℓ . The CEPC panel demonstrates that even small couplings can induce visible deviations owing to its very high luminosity, although the accessible mass range is limited by

the lower center-of-mass energy. The ILC panels illustrate how higher energies broaden the discovery potential, with the 500 GeV setup being particularly effective in probing multi-hundred-GeV Z_ℓ states. Overall, these complementary results emphasize the excellent sensitivity of future e^+e^- colliders to leptophilic gauge interactions.

The dependence of the total cross section on the center-of-mass energy is illustrated in Fig. 4. The CEPC projection (Fig. 4(a)) shows excellent sensitivity near $\sqrt{s} = 240$ GeV due to its very high luminosity, while the ILC panels (Figs. 4(b) and 4(c)) extend the reach to higher energies. In particular, the 500 GeV configuration enhances the prospects for discovering a heavy Z_ℓ by probing deviations from the SM spectrum well into the TeV scale.

The dependence of the total cross section on the leptophilic coupling g_ℓ is shown in Fig. 5. For each collider setup, three configurations are compared: the idealized case without ISR/BS, the ISR-only case, and the full

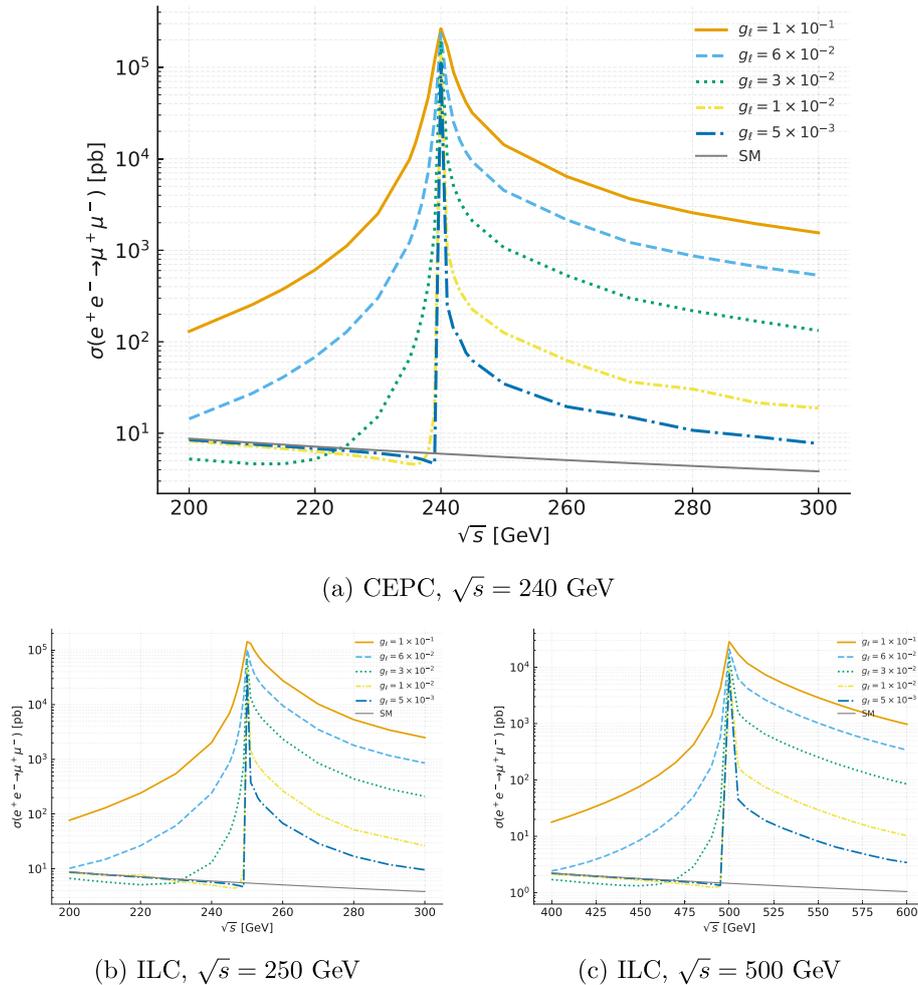


Fig. 4. (color online) Energy scans of the total cross section $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ for representative couplings g_ℓ at future e^+e^- colliders. (a) CEPC at $\sqrt{s} = 240$ GeV (20 ab^{-1} , TDR baseline). (b) ILC at $\sqrt{s} = 250$ GeV (2 ab^{-1} , polarized). (c) ILC at $\sqrt{s} = 500$ GeV. Line styles distinguish the benchmark scenarios. The SM expectation is shown in gray.

ISR+BS simulation. At the CEPC ($\sqrt{s} = 240$ GeV), BS has only a mild effect, while ISR dominates the suppression of the effective cross section. For the ILC, both the 250 and 500 GeV options (Figs. 5(b) and 5(c)) exhibit a stronger sensitivity to ISR+BS, particularly at larger g_ℓ values. These comparisons clearly demonstrate the necessity of including realistic beam effects when estimating discovery sensitivities at future e^+e^- colliders.

The impact of ISR and BS is illustrated in Fig. 6, where the cross section is plotted as a function of M_{Z_ℓ} for $g_\ell = 3 \times 10^{-2}$. At the CEPC (Fig. 6(a)), the resonance appears as a narrow peak. At the ILC-250 (Fig. 6(b)), it is moderately broadened. At ILC-500 (Fig. 6(c)), the peak becomes significantly wider due to stronger beam effects. In all cases, however, the deviation from the SM back-

ground remains visible, showing that ISR and BS reduce but do not eliminate the discovery potential [36, 37].

The invariant mass distribution of the di-muon pair provides a striking signature of a leptophilic resonance. Figure 7 shows the expected spectra for several representative Z_ℓ masses. At the CEPC ($\sqrt{s} = 240$ GeV, Fig. 7(a)), narrow peaks emerge at approximately 180–220 GeV for $g_\ell = 0.02$, clearly separated from the smooth SM background. The ILC-250 configuration ($\sqrt{s} = 250$ GeV, Fig. 7(b)) exhibits similar features near 200 GeV. The ILC-500 setup ($\sqrt{s} = 500$ GeV, Fig. 7(c)) with $g_\ell = 0.03$ demonstrates sensitivity to heavier resonances up to approximately 450 GeV. These distributions highlight the excellent mass resolution and discovery reach achievable at future e^+e^- colliders, with visible Z_ℓ peaks even for

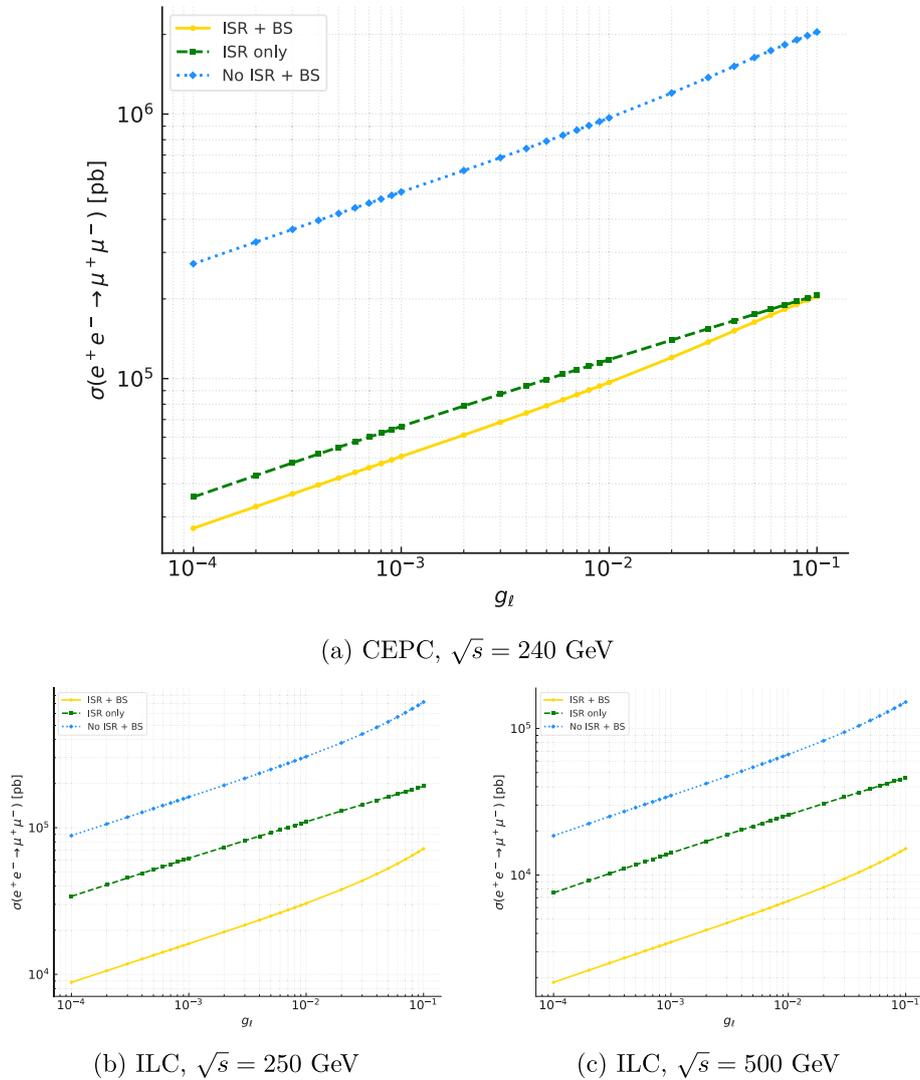


Fig. 5. (color online) Total cross section $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ as a function of the leptophilic coupling g_ℓ for CEPC and ILC setups, illustrating the impact of ISR and BS. (a) CEPC at $\sqrt{s} = 240$ GeV, (b) ILC at $\sqrt{s} = 250$ GeV, and (c) ILC at $\sqrt{s} = 500$ GeV. Solid, dotted, and dash-dot lines correspond to the full ISR+BS simulation, ISR only, and the idealized No ISR+BS case, respectively. Both axes are displayed on logarithmic scales.

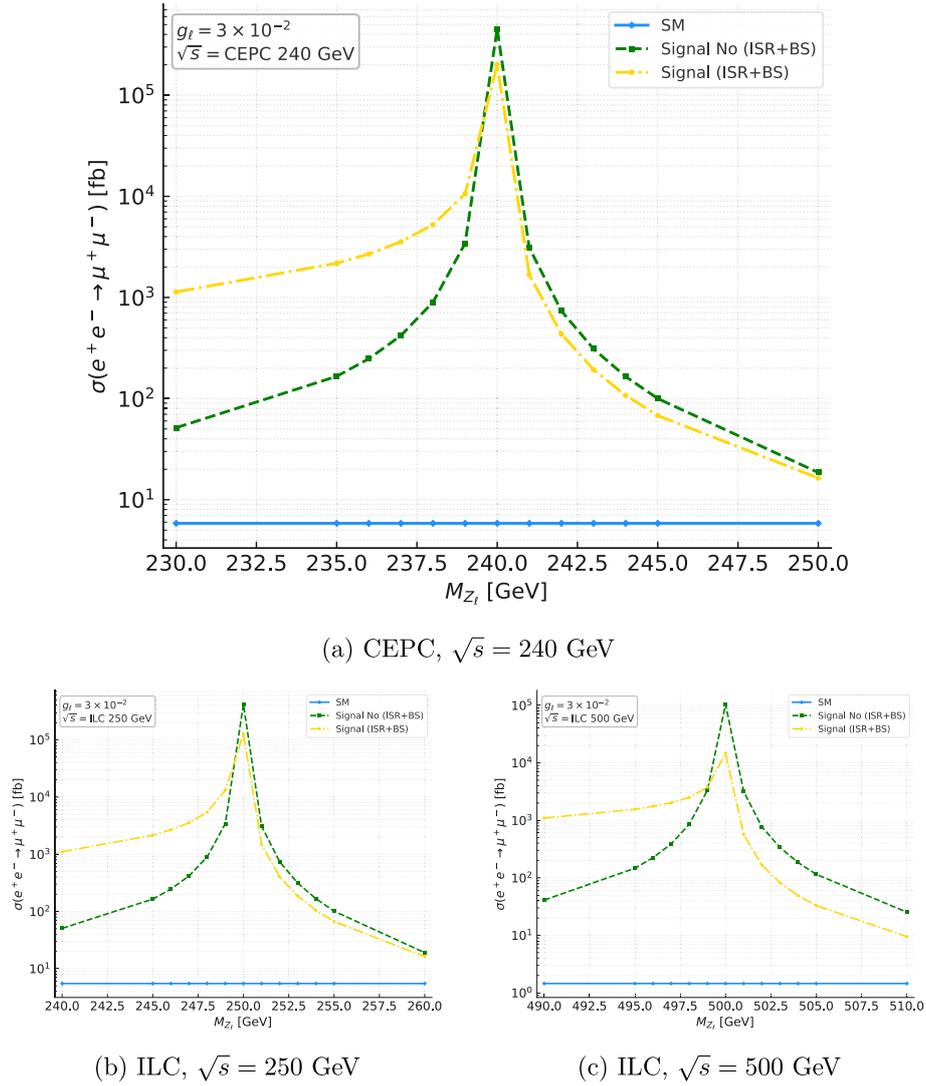


Fig. 6. (color online) Cross section $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ as a function of M_{Z_ℓ} for $g_\ell = 3 \times 10^{-2}$. Comparison of the SM background, signal without ISR/BS, and full ISR+BS. CEPC peak remains narrow, ILC-250 broadens, and ILC-500 widens further though deviation from SM is still distinct.

moderate couplings.

V. RESULTS AND DISCUSSION

Before presenting the numerical projections, it is important to verify that the benchmark scenarios considered here are consistent with existing experimental limits. Current collider searches place only mild constraints on purely leptophilic gauge bosons, since hadron colliders are mostly sensitive to quark-coupled interactions. Dedicated dilepton resonance searches at the Large Hadron Collider (LHC) [38–39] typically assume universal couplings to both quarks and leptons, which are absent in our model. Consequently, direct LHC limits can be substantially relaxed, allowing sub-TeV Z_ℓ masses for couplings below $g_\ell \lesssim 0.1$. Additional constraints from LEP-II con-

tact-interaction analyses [40] and low-energy precision data [36, 41] are also satisfied across the parameter space explored in this study. Therefore, all benchmark points used in the following analysis remain consistent with current bounds and provide a valid basis for discovery projections.

Having established the signal and background framework, we now turn to the projected sensitivities and discovery reaches for the leptophilic photon Z_ℓ at the CEPC and ILC.

The discovery potential of future e^+e^- colliders is summarized in Fig. 8, which displays the 3σ and 5σ significance contours in the (M_{Z_ℓ}, g_ℓ) plane [25, 42–44]. At the CEPC (Fig. 8(a)), couplings down to $g_\ell \approx 10^{-3}$ are accessible for M_{Z_ℓ} up to approximately 220 GeV. The ILC-250 projection (Fig. 8(b)) extends the reach in mass while

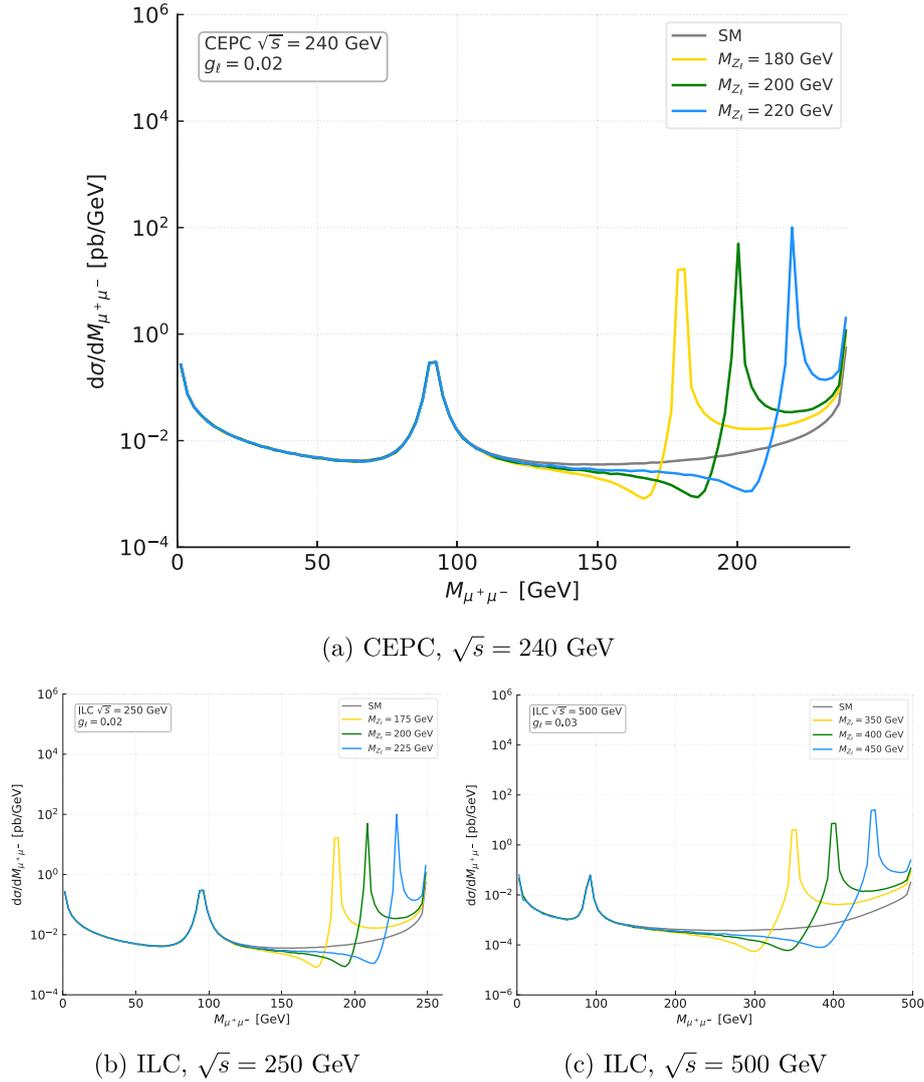


Fig. 7. (color online) Invariant mass distributions of the di-muon system for representative Z_ℓ benchmark masses at future e^+e^- colliders. (a) CEPC at $\sqrt{s} = 240$ GeV with $g_\ell = 0.02$ shows pronounced peaks in the 180–220 GeV range. (b) ILC at $\sqrt{s} = 250$ GeV displays similar structures near 200 GeV. (c) ILC at $\sqrt{s} = 500$ GeV with $g_\ell = 0.03$ extends the sensitivity to resonances up to about 450 GeV. The narrow Z_ℓ resonances stand out clearly above the smooth SM background, illustrating the discovery potential and excellent mass resolution achievable at future lepton colliders.

maintaining similar sensitivity to small couplings. The ILC-500 setup (Fig. 8(c)) pushes the accessible region further into the TeV scale. These results emphasize the complementarity of circular and linear colliders in exploring the leptophilic gauge boson scenario.

In addition to the total cross section, we have also examined differential observables that are sensitive to angular effects, such as the forward–backward asymmetry $A_{\text{FB}} = (\sigma_{\text{F}} - \sigma_{\text{B}})/(\sigma_{\text{F}} + \sigma_{\text{B}})$, where σ_{F} and σ_{B} denote the forward and backward cross sections, respectively. The interference between the SM and leptophilic amplitudes induces characteristic deviations in A_{FB} , particularly near the Z_ℓ resonance. Preliminary simulations indicate that these effects are consistent with the total-rate behavior

discussed above, and can further improve the discrimination power, especially when beam polarization is available at the ILC. A more detailed differential study is left for future work.

For comparison, previous sensitivity estimates at the LEP and early ILC studies typically relied on parton-level simulations without full ISR and BS effects [7, 8, 33]. The present analysis therefore represents a more realistic projection, showing that the clean di-muon channel retains robust sensitivity even once collider-specific effects are included. This improvement is particularly relevant for CEPC, whose very high luminosity enhances the reach well beyond earlier expectations.

Taken together, the results presented in Figs. 2–8

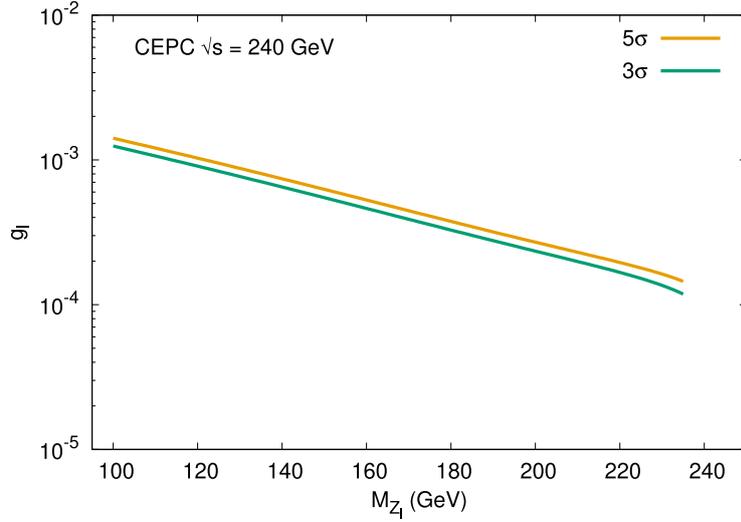
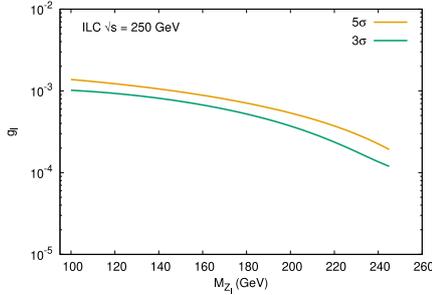
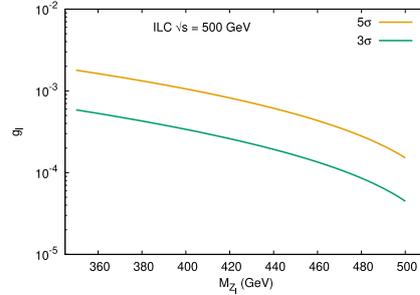
(a) CEPC, $\sqrt{s} = 240$ GeV(b) ILC, $\sqrt{s} = 250$ GeV(c) ILC, $\sqrt{s} = 500$ GeV

Fig. 8. (color online) Projected 3σ and 5σ discovery reaches in the (M_{Z_ℓ}, g_ℓ) plane. (a) CEPC at $\sqrt{s} = 240$ GeV demonstrates sensitivity down to $g_\ell \approx 10^{-3}$ for $M_{Z_\ell} \lesssim 220$ GeV. (b) ILC-250 extends the mass range while maintaining comparable coupling reach, and (c) ILC-500 further improves the mass coverage up to the multihundred-GeV region. The curves correspond to statistical significances computed with full ISR+BS simulation, highlighting the complementarity of circular and linear e^+e^- colliders.

provide a comprehensive picture of the discovery potential for a leptophilic photon Z_ℓ at future e^+e^- colliders. The energy dependence of the cross section highlights the complementary strengths of the CEPC and ILC, with the former providing very high statistics at $\sqrt{s} \approx 240$ GeV and the latter extending the reach toward higher masses through its 250 and 500 GeV options. The variation of the cross section with M_{Z_ℓ} and g_ℓ illustrates how even moderate couplings already produce visible deviations from the SM, even after ISR and BS are taken into account. Invariant-mass spectra confirm that narrow resonances appear as clear peaks over the SM background, consistent with existing bounds from previous e^+e^- experiments [33, 36, 37]. Finally, the projected 3σ and 5σ contours show that the CEPC can probe couplings down to $g_\ell \approx 10^{-3}$ in the sub-TeV region, while the ILC pushes the accessible range further into the TeV domain. These findings underscore the strong complementarity of circular and linear colliders, and establish a solid phenomenological basis

for incorporating leptophilic gauge bosons into future precision programs [11, 12, 25, 26].

VI. CONCLUSIONS

We have presented a dedicated study of the discovery potential for a leptophilic gauge boson Z_ℓ in the clean channel $e^+e^- \rightarrow \mu^+\mu^-$ at future e^+e^- colliders. Incorporating the effects of ISR, BS, and basic detector acceptance, we have provided realistic sensitivity estimates for the CEPC and ILC. The results show that the CEPC, with its very high luminosity at $\sqrt{s} = 240$ GeV, offers broad coverage in the low-mass region, probing couplings down to $g_\ell \approx 10^{-3}$. The ILC extends the accessible Z_ℓ mass range up to the TeV scale through its 250 and 500 GeV stages. This complementarity underscores the unique role of next-generation lepton colliders in testing leptophilic gauge interactions with high precision.

Our analysis established a clear benchmark for the

cleanest leptonic final state and demonstrated that even after including realistic beam effects, the Z_ℓ signal remains clearly visible above the SM background. These findings provide a solid phenomenological basis for future strategies in exploring purely leptophilic scenarios at high-energy colliders.

Compared with previous parton-level estimates and earlier sensitivity projections from LEP and ILC studies, the present work offers a more realistic evaluation by incorporating ISR, BS, and acceptance effects. In this respect, our results represent the first direct side-by-side comparison of the CEPC and ILC in the context of a purely leptophilic gauge boson. The projections presented here highlight the advantage of the CEPC in probing very small couplings at low mass, and the complementary role of the ILC in extending the discovery reach well into the multi-hundred GeV domain.

From a broader perspective, the analysis provides timely input into the global discussion on the physics potential of future lepton colliders. In particular, the CEPC, as a central project in China, is shown to deliver world-leading sensitivity to new leptonic forces in the sub-TeV regime, while the ILC offers a complementary path at higher energies. Taken together, these findings underscore the importance of pursuing both circular and linear collider options, and establishing a strong phenomenological basis for including leptophilic gauge bosons in the physics case of next-generation facilities.

DATA AVAILABILITY

All data generated and analyzed in this study are included in the article. Additional simulation inputs and numerical results are available from the corresponding author upon reasonable request.

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